

Fixed points and their types

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Annotatsiya. Ushbu maqolada dinamik sistemalarning qo'zg'almas nuqtalari va ularning turlari Lagranj teoremlari yordamida isbotlangan o'rganilgan

Abstract. In this article, the fixed points of dynamic systems and their types are studied, proved using Lagrange's theorems.

Kalit so'zlar. Lagranj teoremasi, Giperbolik nuqta, qo'zg'almas nuqta, dinamik sistemalar

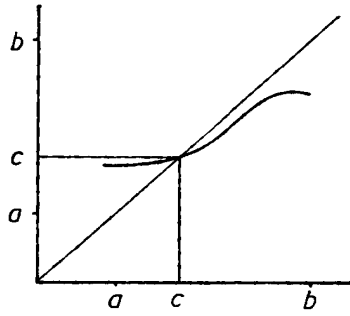
Key words. Lagrange's theorem, hyperbolic point, fixed point, dynamical systems

Definition 1. If the equality $f(x) = x$ is fulfilled for a point x , the point x is called a fixed point of the function $f(x)$.

Lemma 1. Let the given function $f: I \rightarrow I$ be continuous, then the function $f(x)$ has at least one fixed point in the interval I .

Proof. Let $f(x) - x = g(x)$. It is known that $g(x)$ is continuous in I . Let $f(a) > a, f(b) < b$ be. From this, $g(a) > 0, g(b) < 0$,

According to the mean value theorem, there exists such a point $c \in [a, b]$ that $g(c) = 0$ becomes $g(c) = f(c) - c. g(c) = 0 \Rightarrow f(c) = c$.



Picture 1

Lemma 2. If the function $f: I \rightarrow I$ is continuous and $|f'(x)| < 1$ for $\forall x \in I$, then the function f has a unique fixed point belonging to I . Also, for the $\forall x, y \in I, x \neq y$

$\forall x, y \in I, x \neq y$ inequality is appropriate.

Proof. By Lemma 1, $f(x)$ has at least one fixed point. Let x and y ($x \neq y$) be fixed points. According to Lagrange's theorem, there exists a point c between the points x and y ,

$$f'(c) = \frac{f(y) - f(x)}{y - x} = 1$$

But this equality contradicts the inequality $|f'(c)| < 1$ for $\forall c \in I$. So our assumption is wrong. $x = y$ will be. That is, the function $f(x)$ has unique fixed point in I .

In proving the second part of the lemma, we again use Lagrange's theorem. $\forall x, y \in I, x \neq y$,

$$|f(y) - f(x)| = |f'(c)||y - x| < |y - x| \text{ for } s$$

Definition 2. Let the point x be a fixed point of $f(x)$. A point x is called a periodic point with period n if $f^n(x) = x$.

Example 1. Let's find fixed points of $f(x) = x^3$ functions.

We find the roots of equation $x^3 - x = 0$.

$$x^3 - x = 0$$

$$x(x^2 - 1) = 0$$

$$x_1 = 0, x_2 = 1, x_3 = -1$$

So, the points 0, 1, and -1 are fixed points of the function $f(x)$.

Example 2. Let's find the fixed points of the function $f(x) = x^2 - 1$.

$$x^2 - 1 = x$$

$$x^2 - x - 1 = 0$$

$$x_{1,2} = (1 \pm \sqrt{5})/2$$

So, the fixed points of the given function $f(x)$ are $x_{1,2} = (1 \pm \sqrt{5})/2$ points.

In other words, when finding fixed points, it is necessary to find the points of intersection of the graph of the given function with the graph of the function $x = y$.

Hyperbolic points.

Functions $f(x) = x$ and $f(x) = -x$ are different in the theory of dynamical systems. An unusual feature of such reflections is that all their points are periodic. Most reflections do not have this feature. Therefore, we introduce the concept of hyperbolicity.

Let us be given a function $f(x)$ defined on the real domain.

Definition 3. Let the point p be a periodic point with n periods. If $|(f^n)'(p)| \neq 1$, then n is called a hyperbolic point.

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